

$$1. \quad (a) \int (12x^2 + 10)(2x^3 + 5x + 5)^9 dx = \int 2(6x^2 + 5)(2x^3 + 5x + 5)^9 dx =$$

$$\int 2u^9 du = \frac{2u^{10}}{10} + C = \frac{(2x^3 + 5x + 5)^{10}}{5} + C$$

$$u = 2x^3 + 5x + 5 \\ du = (6x^2 + 5)dx$$

$$(b) \int \frac{8x^2}{\sqrt{x^3 + 2}} dx = \int \frac{8}{\sqrt{u}} * \frac{1}{3} du = \int \frac{8}{3} u^{-\frac{1}{2}} du = \frac{8}{3} \frac{u^{\frac{1}{2}}}{\frac{1}{2}} + C = \frac{16}{3} \sqrt{u} + C = \frac{16}{3} \sqrt{x^3 + 2} + C$$

$$u = x^3 + 2 \\ du = 3x^2 dx \\ \frac{du}{3} = x^2 dx$$

$$2. \quad (a) \int (x^3 + 2) \cos(x^4 + 8x) dx = \int \frac{1}{4} \cos(u) du = \frac{1}{4} \sin(u) + C = \frac{1}{4} \sin(x^4 + 8x) + C$$

$$u = x^4 + 8x \\ \frac{du}{4} = (x^3 + 2)dx$$

$$(b) \int \frac{3e^{3x} - 2e^{-2x}}{e^{3x} + e^{-2x}} dx = \int \frac{1}{u} du = \ln(u) + C = \ln(e^{3x} + e^{-2x}) + C$$

$$u = e^{3x} + e^{-2x} \\ du = (3e^{3x} - 2e^{-2x})dx$$

$$3. \quad (a) \int_0^A 4e^{2x} - 10 \sin(2x) dx = (2e^{2x} + 5 \cos(2x)) \Big|_0^A = (2e^{2A} + 5 \cos(2A)) - (2 + 5) = 2e^{2A} + 5 \cos(2A) - 7$$

$$(b) \int_B^5 \frac{7}{x} - \frac{2}{x^2} dx = 7 \ln(x) + 2x^{-1} \Big|_B^5 = 7 \ln(5) + \frac{2}{5} - \left(7 \ln(B) + \frac{2}{B} \right) \text{ or } 7 \ln(5) + \frac{2}{5} - 7 \ln(B) - \frac{2}{B}$$

$$4. \quad \int_1^B x^2 e^{x^3+2} dx = \int_{x=1}^{x=B} \frac{1}{3} e^u du = \frac{1}{3} e^u \Big|_{x=1}^{x=B} = \frac{1}{3} e^{x^3+2} \Big|_1^B = \frac{1}{3} e^{(B^3+2)} - \frac{1}{3} e^3$$

$$u = x^3 + 2 \\ \frac{du}{3} = x^2 dx$$

5. problem was omitted. To solve this problem, you need to know the size of the population in 1990.

6. note: to find the y-value use the fundamental theorem of calc.

$$\int_0^2 f'(x) dx = f(2) - f(0)$$

$$132 = f(2) - 20$$

$$f(2) = 152$$

other values computed in a similar manner.

(a) local minimum: $(20, -28)$

(b) local maximum: $(8, 152)$ and $(32, 172)$