

Section 16.8: Additional Problems

1. Let $\mathbf{F} = \langle xz, 2xy, 3xy \rangle$. Evaluate $\int_C \mathbf{F} \cdot d\mathbf{r}$ where C is the boundary of the part of the plane $3x + y + z = 3$ in the first octant and C is oriented counterclockwise as viewed from above.
2. Use Stokes's Theorem to evaluate $\iint_S \text{curl } \mathbf{F} \cdot d\mathbf{S}$
 $\mathbf{F} = \langle yz^3, \sin(xyz), x \rangle$
 S is the part of the paraboloid $y = 1 - x^2 - z^2$ that lies to the right of the xz -plane, oriented toward the xz -plane.
3. Use Stokes's Theorem to evaluate $\iint_S \text{curl } \mathbf{F} \cdot d\mathbf{S}$
 $\mathbf{F} = \langle xyz, xy, x^2yz \rangle$
 S consists of the top and the four sides (but not the bottom) of the cube with vertices $(\pm 1, \pm 1, \pm 1)$, oriented outward. Hint: Think about the last example in the lecture.