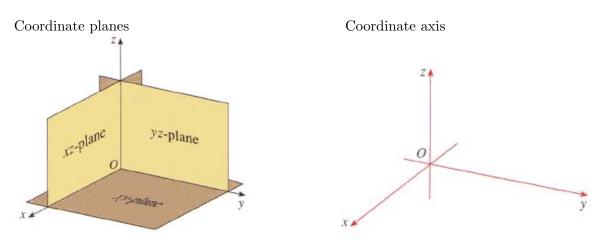
Section 12.1: Three Dimensional Coordinate System



Distance formula: The distance $|P_1P_2|$ between the points $P_1(x_1, y_1, z_1)$ and $P_2(x_2, y_2, z_2)$ is

$$|P_1P_2| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

Shapes in 3-space

Cylindrical surfaces

An equation that only two of the variables x, y, and z represents a curve when graphed in \Re^2 and a cylindrical surface when graphed in \Re^3 .

To graph the cylindrical surface, first graph the equation in the coordinate plane of the two variables and then translate that graph with respect to the axis of the missing variable.

Example: Sketch the graph of the **parabolic cylinder** $y = x^2 + 1$ in \Re^3 .

(b) What is the intersection of S with the xz-plane?

(c) What is the intersection of S with the yz-plane?

(d) What is the intersection of S with the xy-plane?

Plane

The equation of a plane is of the form ax + by + cz = d with a, b, c, and d are constants.

Example: Find the points where the plane 3x + 5y + 2z = 30 intersects the coordinate axis. Sketch a graph of this plane.

$$(x-h)^{2} + (y-k)^{2} + (z-l)^{2} = r^{2}$$

Example: Find an equation of a sphere with center at (3, 4, -1) and a radius of 7.

Example: Use the sphere $(x-3)^2 + (y-4)^2 + (z+7)^2 = 25$ to answer the following. A) Find the intersection of the sphere and the xz coordinate plane.

B) What is the distance from the center of the sphere to the xz-plane?

C) How far is the center from the x-axis?

 $2x^2 + 2y^2 + 2z^2 + 8y - 6z = 4$

Example: Describe the following region of \Re^3 represented by the equation(s) $x^2 + z^2 = 10, y = 4$