

Final Exam Information

You are encouraged to double check this document to make sure that I didn't leave anything off.

• Section 14.7

Absolute max/min over a closed and bounded region.

• Section 16.1

vector fields

being able to draw/recognize a vector field

gradient vector field

conservative vector field

potential function for a vector field.

• Section 16.2

line integral of f along C .

- line integral with respect to arc length
- how to compute ds in both two dimension and three dimension.
- is the orientation of C important in this type of line integral?

parametrize a line segment from start point to end point.

line integral of a function over a piecewise-smooth path is the sum of the line integrals of the function over each section of the path.

line integral of f with respect to x and line integral of f with respect to y and line integral of f with respect to z

- is the orientation of C important in this type of line integral?

Line integrals in a vector field.

- is the orientation of C important in this type of line integral?
- what is the relationship between a line integral of a vector field F along a path C to the line integral of a function f with respect to x , with respect to y , and with respect to z along a path C .

• Section 16.3

Fundamental theorem of line integrals

- when can this be used? i.e. what types of vectors fields can this theorem be applied in?

Independent of path

- any closed path(start and stop at the same point) for a line integral that is independent of path is 0.

determining if a two dimension vector field is conservative/not conservative

simple curve

simply-connect region

finding a potential function for a conservative vector field.

• Section 16.4

Green's Theorem:

- positive orientation(counter-clockwise)
- closed region

computing the area of region D (a double integral) by using a line integral where $Q_x - P_y = 1$

common methods

$$P = 0 \text{ and } Q = x$$

$$P = -y \text{ and } Q = 0$$

$$P = -0.5y \text{ and } Q = 0.5x$$

how to fix a path that is not positively orientated.

how to fix a path that is not closed.

• Section 16.5

curl F

what does it mean if the curl $F = \langle 0, 0, 0 \rangle$

divergence of F

div curl $F = ?$

• Section 16.6

parameterize a surface

tangent plane for a surface that has been parameterized

short cut for finding a cross product for particular parameterizations.

compute surface area of a region that is parameterized.

• Section 16.7

not in a vector field

- surface integral of a function over a surface S .
- surface integral where S is the boundary of a solid.

in a vector field F

- oriented surface
- picking the cross product that matches the orientation of the surface
- for a closed surface, positive orientation is where the normal vectors point outward.
- surface integral of F over S . also called the flux of F across S .
- surface integral of F over a closed surface.

- **Section 16.8**

stokes' theorem

- **Section 16.9**

divergence theorem

Any additional topic/information covered in these sections.