

Section 3.4: Additional Problems

Problems 1-5 refer to the functions f and g that satisfy the properties as shown in the table. Find the indicated quantity.

x	$f(x)$	$f'(x)$	$g(x)$	$g'(x)$
0	1	-3	3	5
1	2	6	7	11
2	-5	0	2	10
3	4	-1	-4	8

1. $H'(0)$ if $H(x) = f(g(x))$
2. $J'(-1)$ if $J(x) = f(x^2)$
3. $K'(2)$ if $K(x) = (x^2 + g(x))^3$
4. $J'(1)$ if $J(x) = (x^3 + 1)g(3x)$
5. $H'(1)$ if $H(x) = g(x^2 + f(x))$

For problems 6-8, find the values of x where the tangent line is horizontal.

6. $y = x^2(x - 3)^4$
7. $y = (x + 1)^2(x - 3)^3$
8. $y = (5 - x^2)^7(7x + 1)^4$

In problems 9-18, find each derivative. You do not have to simplify.

9. $f(x) = (2x + 1)\sqrt{x^2 + 1}$
10. $f(x) = e^{3x+e^x}$
11. $f(x) = (x^2 + 6x + 1)^4$
12. $f(x) = 3^{x^2+5x+1}$
13. $y = \frac{e^{x^2+4x}}{e^{4x+5}}$
14. $f(x) = (x^3 + 5x + 9)^{\frac{3}{2}}$
15. $f(x) = \sqrt[3]{x^3 + \frac{1}{x^3}}$

16. $f(x) = (3x^5 - 1)^4(x^3 + 2)^3$

17. $f(x) = [(x^4 - 7x^2)^6 + 4x^3]^5$

18. $f(x) = (2x^3 + 7x)e^{(x^4+3x^2+1)}$

19. Find the derivative and simplify the answer.

$$y = \frac{x^2 + 1}{\sqrt{x^2 + 2}}$$

20. Find $D^{1047} \sin(3x + 1)$ or $\frac{d^{1047}}{dx^{1047}} \sin(3x + 1)$