Solutions to Sample problems 2.

1. feasible region labled F.R.

2. max at $(2.5,7.5)$ maximum value is 25 .
3. min at $(4.5,0)$ minimum value is 4.5 .
4. $x=$ the number of batches of Vanilla
$y=$ the number of batches of Mocha
$z=$ the number of batches of Strawberry
$\max P=3 x+2 y+4 z$
constraints:
$2 x+y+z \leq 220$
$x+y+2 z \leq 120$
$2 x+2 y+2 z \leq 200$
$z \leq 10$
$x \geq 0, y \geq 0, z \geq 0$
5. The answers are listed in column form.

| F | F | T |
| :---: | :---: | :---: |
| T | F | F |
| T | T | F |
| F | F | F |

6. (a) $\emptyset,\{a\},\{b\},\{c\},\{a, b\},\{a, c\},\{c, b\}$, and A.
(b) $\emptyset,\{a\},\{b\},\{c\},\{a, b\},\{a, c\},\{c, b\}$
(c) any two of the subsets above such that their intersection is empty.
7. part a)

part b)

8. (a) $\left(A \cap B^{C} \cap C^{C}\right) \cup\left(B \cap A^{C} \cap C^{C}\right)$
(b) $\left.\left(A^{C} \cap C\right) \cup\left(B^{C} \cap C\right)=\left(A^{C} \cup B^{C}\right) \cap C\right)=$ $(A \cap B)^{C} \cap C$
9. (a) $\{1,2,4,6,7,8\}$
(b) $\{2,4,8\}$
(c) $\{3,5,9\}$
10. see the solutions for the on-line suggest homework for these answers.
11. (a) figure to the side
(b) 150
(c) 221
(d) 19
(e) 110
(f) 105

12. 3
13. (a) 17576000
(b) 12167000
(c) 12164000
14. $53 \frac{1}{3}$ minutes
15. (a) 15504 (b) 1860480
16. (a) 126
(b) 21
(c) 70
17. 336
18. (a) 12 (b) 198 (c) 100
19. $64,864,800$
20. (a) $S=\{(1, h),(1, t),(2, h),(2, t),(3, h)$, $(3, t),(4, h),(4, t)\}$
(b) no they are not mutually exclusive since $(2, h)$ is in both E and F .
(c) Any two subsets of S that are disjoint.
