

# Spring 2012 Math 151

## Week in Review # 7

sections: 4.2, 4.3, 4.4

*courtesy: Joe Kahlig*

### Section 4.2

1. Determine if the function is one-to-one.

$$y = \sqrt[3]{x^2 + 1}$$

2. Show that the function is one-to-one and find the inverse.

(a)  $f(x) = \frac{1 - 4x}{3x + 5}$

(b)  $f(x) = \sqrt[3]{x^3 + 7}$

3. Assume that the function  $f$  is a one-to-one function with inverse  $g$ . Compute a formula for  $g'(x)$  based on  $f$ .

4. If  $g$  is the inverse of the function  $f$ , compute  $g'(2)$ .

$$f(x) = x^5 - x^3 + 2x$$

5. If  $g$  is the inverse of the function  $f$ , compute  $g'(6)$ .

$$f(x) = 5 + xe^{(x^2 - 2x + 1)}$$

### Section 4.3

6. Evaluate:  $4^{2\log_4 9}$

7. Find the domain of this function.

$$y = \ln(x^2 - 9)$$

8. Use the fact that  $\log_a 2 = 0.38$ ,  $\log_a 3 = 0.63$ , and  $\log_a 5 = 0.88$  to compute these logarithms.

(a)  $\log_a 20$

(b)  $\log_a \left( \frac{81}{a^3} \right)$

9. Solve for  $x$ .

(a)  $4e^{(3x+2)} = 12$

(b)  $5(7)^{4x} = 3$

(c)  $\log(x - 2) + \log(x + 4) = \log 7$

(d)  $\log_x(6x - 5) = 2$

(e)  $\log_{27}(4\log_2(5x - 4) - 17) = \frac{1}{3}$

## Section 4.4

For problem 10-16, find the derivatives of these functions.

10.  $y = \log_5(7 - 4x) + 3^{\sec(x)}$

11.  $y = [\ln(x^4 + 5x)]^{\frac{4}{3}}$

12.  $y = \ln(\ln(3x + 1))$

13.  $y = 7^{x^2} \log(x^4 + 1)$

14.  $y = \ln \sqrt{\frac{x^2 + 5}{5x - 8}}$

15.  $y = (x^2 + 3)^{\cos(2x)}$

16.  $y = \frac{(2x^6 + 4)^5}{(7x^2 + 5)^3}$