## Week in Review \#4

1. $x+y>20$
$x+2 y \geq 24$
$3 x-2 y>0$
2. The corner points are labeled in the picture.


| c.p. | $F=4 x+2 y$ |
| :---: | :---: |
| $\mathrm{~A}\left(\frac{8}{9}, \frac{70}{9}\right)$ | $\frac{172}{9} \approx 19.1111$ |
| $\mathrm{~B}(32,0)$ | 128 |
| $\mathrm{C}(8,0)$ | 32 |
| $\mathrm{D}(3,2.5)$ | 17 |

The maximum value of F is 128 and occurs at point $B$.
3. Corner points are D, E, and F. Since the region is unbounded create two imaginary corner points: $\mathrm{L}(0,20)$ and $\mathrm{K}(10,7)$.

| c.p. | D | E | F | L | K |
| :---: | :---: | :---: | :---: | :---: | :---: |
| f | 15 | 15 | 18 | 20 | 27 |

min value of 15
location of minimum: point D and E and all points between them on a straight line. ie. $\overline{D E}$ or $\overline{E D}$
4. Corner points are A, B, and C. Since the region is unbounded create two imaginary corner points: $\mathrm{J}(0,25)$ and $\mathrm{K}(13,25)$
(a) Values:

| A | B | C | J | K |
| :---: | :---: | :---: | :---: | :---: |
| -72 | 22 | 125.5 | -75 | 55 |

maximum value is 125.5
location of the maximum is C .
(b) Values:

| A | B | C | J | K |
| :---: | :---: | :---: | :---: | :---: |
| 96 | 36 | 45 | 100 | 139 |

Since the maximum value is at the imaginary point K , there is no solution for this problem.
(b) $A \cup B=\{0,2,3,4,6,8,9\}$
$n(A \cup B)=7$
(c) $C^{C}=\{0,2,4,6,8\}$
$A \cup C^{C}=\{0,2,3,4,6,8,9\}$
(d) $A \cap B \cap C=\phi$
(e) $A \cap C=\{3,9\}$ $(A \cap C)^{C}=\{0,1,2,4,5,6,7,8\}$
$(A \cap C)^{C} \cap B=\{0,2,4,6,8\}$
(f) $2^{5}=32$
(g) $2^{5}-1=31$
(h) no, they have 0 and 6 in common.
(i) yes
7. (a) $A \cup B \cup C$

(b) $(B \cup C)^{C}$

(c) $\left(A^{C} \cap B\right) \cup C$

8. (a) i. The A\&M students that drink sprite or do not drink coffee.
ii. The male students at A\&M that drink Dr. Pepper or Sprite.
(b) i. $F \cap S \cap C^{C}$
ii. $C \cup D^{C}$
5. $\{E, N, C, Y, L, O, P, D, I, A\}$
6. (a) $n(A)=4$

